

1952

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J.E. Grafius

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## Recommended Citation

Grafius, J.E., "A Statistical Model for Estimating Components of Genetic Variance in Bulk Yield Tests of Self-Pollinated Small Grains" (1952). *Agricultural Experiment Station Technical Bulletins*. 21.  
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Technical Bulletin No. 9

SPC 76 1952

May 1952

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## ACKNOWLEDGMENT

The author wishes to thank Professors H. B. MacDougal and O. E. Walder of South Dakota State College for their assistance. Credit also is due Dr. R. E. Comstock of the North Carolina State College for his critical review of this manuscript and for his many helpful suggestions.

A STATISTICAL MODEL FOR ESTIMATING THE COMPONENTS OF GENETIC VARIANCE IN BULK YIELD TESTS OF SELF-POLLINATED SMALL GRAINS

J. E. GRAFIUS<sup>1</sup>

Comstock and Robinson (1)<sup>2</sup> have given a statistical model for the isolation of the components of genetic variance in populations of biparental progenies. Their model has made possible the construction of one for self-pollinated progenies to be applied to the method of small grain breeding (3) (4), wherein large numbers of bulked  $F_2$  and  $F_3$  progenies are tested for yielding ability. Inasmuch as the genetic variance of high yielding progenies will be due to both additive and non-additive genetic effects, it is important that these effects be separated.

In self-pollinated small grains, the final objective of the breeding program is an isogenic line. Hence the additive, or heritable genetic variance is highly important, while the non-additive genetic variance is, in general, not usable.

*Limiting Assumptions and Definitions*

The genetic models to be proposed assume that the genes at the separate loci are randomly distributed in the population of homozygous lines from which the parents were drawn at random.

It is also assumed that there is no epistasis and (for the purposes of summation) that genes 1 to  $n$  have equal effect. In the absence of bias caused by epistasis, linkage will not interfere with the conclusions that can be drawn from the model for the analysis of variance. This analysis is based on cross means, and in the absence of epistasis the cross mean will be the result of the average effect of the segregating loci irrespective of the linkage relationships.

The additive genetic variance at the  $a$ th locus has been defined (1) (6) as that part of the variance of the genetic effects attributable to regression on the number of  $A$  genes in the genotype. Conversely, the variance of the genetic deviations from regression represents the

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<sup>2</sup> Figures in parentheses refer to "Literature Cited," p. 13.

variance due to deviations from the additive scheme caused by dominance and epistasis. The additive genetic variance may, in turn, be divided into an unfixable and a fixable portion. It is this latter part of the additive genetic variance that may be retained in an isogenic line.<sup>3</sup>

*Estimations of Components of Genetic Variance Within Crosses  
Between Self-Pollinated Varieties*

After the genetic model presented by Comstock and Robinson, let  $y$  be the mean effects of the genotype,  $x$  be the number of  $A$ 's in the genotype,  $u$  be the frequency of  $A$ , and  $v = (1 - u)$  be the frequency of  $a$  in the population. Then for an  $F_2$ , the genotypes for a single locus will have the distribution shown in Table 1.

TABLE 1. THE DISTRIBUTION OF GENOTYPES AND THEIR MEAN EFFECTS FOR AN  $F_2$  POPULATION

Genotype	Genotypic frequency	Frequency of $A$ $x$	Mean effects $y$
$AA$	$u_a^2$	2	$d_a$
$Aa$	$2u_a v_a$	1	$h_a$
$aa$	$v_a^2$	0	$-d_a$

Before proceeding to calculate the  $F_2$  variance it is necessary to define certain symbols. For a single segregating locus let

$$\sigma_{y_a}^2 = \text{the total genetic variance}$$

$$\sigma_{d_a}^2 = \text{the additive genetic variance}$$

$$\sigma_{h_a}^2 = \text{the non-additive genetic variance}$$

$$Cov_{x_a y_a} = \text{the covariance of } x_a \text{ and } y_a$$

$$\text{and } \sigma_{x_a}^2 = \text{the variance of } x_a.$$

Upon summing the variance from a series of such segregating loci

$$\sigma_y^2 = \sum_1^n \sigma_{y_a}^2, \quad \sigma_d^2 = \sum_1^n \sigma_{d_a}^2, \quad \sigma_h^2 = \sum_1^n \sigma_{h_a}^2, \quad \sigma_x^2 = \sum_1^n \sigma_{x_a}^2,$$

$$\text{and } Cov_{xy} = \sum_1^n Cov_{x_a y_a}$$

<sup>3</sup> For example, the additive genetic variance for the  $a$ th locus in an  $F_2$  may be written  $2\sum u_a v_a [d_a + h_a(v_a - u_a)]^2$ . The term containing  $d_a^2$  is fixable, but the terms containing  $h_a$  are not fixable.

Working from Table 1 it was found that

$$\begin{aligned}
 \sigma_{y_a}^2(F_2) &= d_a^2(u_a^2 + v_a^2) + 2u_a v_a h_a^2 - \left[ (u_a - v_a) d_a + 2u_a v_a h_a \right]^2 \\
 &= d_a^2(2u_a v_a) + 4u_a v_a d_a h_a (v_a - u_a) + 2u_a v_a h_a^2(1 - 2u_a v_a) \\
 &= 2u_a v_a \left[ d_a + h_a(v_a - u_a) \right]^2 + 4u_a^2 v_a^2 h_a^2 \\
 \sigma_y^2(F_2) &= 2 \sum u_a v_a \left[ d_a + h_a(v_a - u_a) \right]^2 + 4 \sum u_a^2 v_a^2 h_a^2 \quad [1]
 \end{aligned}$$

Equation [1] gives the total  $F_2$  genetic variance. By definition, the additive genetic variance at the  $a$ th locus equals

$$\frac{\left[ Cov_{x_a y_a}(F_2) \right]^2}{\sigma_{x_a}^2}$$

This may be obtained as follows

$$\begin{aligned}
 Cov_{x_a y_a}(F_2) &= 2u_a^2 d_a + 2u_a v_a h_a - \left[ (2u_a^2 + 2u_a v_a)(u_a^2 d_a + 2u_a v_a h_a - v_a^2 d_a) \right] \\
 &= 2u_a v_a \left[ d_a + h_a(1 - 2u_a) \right] \\
 &= 2u_a v_a \left[ d_a + h_a(v_a - u_a) \right] \\
 \sigma_{x_a}^2 &= u_a^2(2)^2 + 2u_a v_a(1)^2 - \left[ 2u_a^2 + 2u_a v_a \right]^2 = 2u_a v_a, \quad \sigma_r^2 = 2 \sum u_a v_a \\
 \sigma_{d_a}^2(F_2) &= \frac{\left[ Cov_{x_a y_a}(F_2) \right]^2}{\sigma_{x_a}^2} = \left\{ 2u_a v_a \left[ d_a + h_a(v_a - u_a) \right] \right\}^2 \\
 \sigma_d^2(F_2) &= 2 \sum u_a v_a \left[ d_a + h_a(v_a - u_a) \right]^2 \quad [2]
 \end{aligned}$$

The non-additive genetic variance in [1] may be obtained by subtraction

$$\begin{aligned}
 \sigma_{h_a}^2(F_2) &= \sigma_{y_a}^2(F_2) - \sigma_{d_a}^2(F_2) = 4u_a^2 v_a^2 h_a^2 \\
 \sigma_h^2(F_2) &= 4 \sum u_a^2 v_a^2 h_a^2 \quad [3]
 \end{aligned}$$

Similarly it was found that for the variance of the  $F_3$  family means that

$$\sigma_v^2(\bar{F}_3) = 2\Sigma u_a v_a \left[ d_a + \frac{h_a}{2} (v_a - u_a) \right]^2 + \Sigma u_a^2 v_a^2 h_a^2 \quad [4]$$

$$\sigma_d^2(\bar{F}_3) = 2\Sigma u_a v_a \left[ d_a + \frac{h_a}{2} (v_a - u_a) \right]^2 \quad [5]$$

$$\sigma_h^2(\bar{F}_3) = \Sigma u_a^2 v_a^2 h_a^2 \quad [6]$$

and that for the variance of the  $F_4$  family means from unselected  $F_3$  families that

$$\sigma_v^2(\bar{F}_4) = 2\Sigma u_a v_a \left[ d_a + \frac{h_a}{4} (v_a - u_a) \right]^2 + \frac{\Sigma u_a^2 v_a^2 h_a^2}{4} \quad [7]$$

$$\sigma_d^2(\bar{F}_4) = 2\Sigma u_a v_a \left[ d_a + \frac{h_a}{4} (v_a - u_a) \right]^2 \quad [8]$$

and that

$$\sigma_h^2(\bar{F}_4) = \frac{\Sigma u_a^2 v_a^2 h_a^2}{4} \quad [9]$$

In a cross of two homozygous lines where  $u = v = 1/2$ , equations [1-9] will reduce to terms of  $d^2$  and/or  $h^2$ . For example, equation [1]

$$\text{will reduce to } \frac{1}{2} \Sigma d_a^2 + \frac{1}{4} \Sigma h_a^2$$

which is the expression obtained by Fisher, Tedin and Immer (2) for the total  $F_2$  genetic variance. The reduced equation [7] equals

$$\frac{1}{2} \Sigma d_a^2 + \frac{1}{64} \Sigma h_a^2.$$

This can be verified by following the method given by Mather (5).

If  $u \neq v \neq \frac{1}{2}$  and  $h \neq 0$ , the contributions made by  $d$  and  $h$  are not completely separable. Under these conditions  $\sigma_d^2$  will include some of the effects of  $h$  and  $\sigma_h^2$  will be correspondingly less than the summed effects of all the squared  $h$  deviations (5).

#### *Estimation of the Composition of Variance between Self-Fertilized Bulk Progenies from Different Crosses*

Let  $j$  homozygous lines be used as female parents to be crossed with each of  $k$  males. The bulk progeny from each cross will be grown



in  $r$  replications. The variance can then be partitioned as shown in Table 2.

TABLE 2. ANALYSIS OF VARIANCE BETWEEN SELF-FERTILIZED BULKED PROGENIES FROM CROSSES OF HOMOZYGOUS LINES

Source of variance	d.f.	m.s.	Expectations of m.s.
Replication	$r-1$		
Crosses	$jk-1$		
Between progeny of different $\delta \delta$	$k-1$	$M_1$	$\sigma^2 + r\sigma_{m \times f}^2 + rj\sigma_m^2$
Between progeny of different $\varphi \varphi$	$j-1$	$M_2$	$\sigma^2 + r\sigma_{m \times f}^2 + rk\sigma_f^2$
Interaction	$(j-1)(k-1)$	$M_3$	$\sigma^2 + r\sigma_{m \times f}^2$
Error	$(r-1)(jk-1)$	$M_4$	$\sigma^2$
Total	$jkr-1$		

KEY TO TABLE 2

$\sigma^2$  = environmental variance

$\sigma_m^2$  = the variance of male effects

$\sigma_f^2$  = the variance of female effects

$\sigma_{m \times f}^2$  = the variance due to the interaction of male and female effects

The four components of variance can be estimated from the appropriate mean squares. To illustrate,

$$(M_1 - M_3) / rj \approx \sigma_m^2.$$

The genetic model for Table 2 will be as follows:

Starting with homozygous parents, the frequency of gene  $A-a$  will also equal the frequency of the genotype  $AA$  and  $aa$ . Let  $u$  equal the frequency of the  $AA$  genotype and  $v = (1-u)$  the frequency of the  $aa$  genotype in the hypothetical parental population. Then, on the average,<sup>4</sup>  $u$  of the males and females will be  $AA$  and  $v$  will be  $aa$ . An  $AA$  female may have  $F_1$  progeny of two types,  $AA$

<sup>4</sup> Where the males and females are picked at random.

and  $Aa$  with a frequency of  $u^2$  and  $uv$  respectively. An  $aa$  female may have  $F_1$  progeny of two types  $Aa$  and  $aa$  with frequencies of  $uv$  and  $v^2$  respectively. The same reasoning applies to the male parents.

TABLE 3. MEAN EXPRESSIONS FOR  $F_1$  PROGENIES FROM CROSSES BETWEEN HOMOZYGOUS LINES

Parental genotype		Means of progeny from female parent	
Female	Male		
	$AA$ $u$	$aa$ $v$	
	Progeny means		
$AA$ $u$	$\bar{y}_a = d_a$	$h_a$	$u_a d_a + v_a h_a$
$aa$ $v$	$h_a$	$-d_a$	$u_a h_a - v_a d_a$
Means of progeny from male parents	$u_a d_a + v_a h_a$	$u_a h_a - v_a d_a$	Grand mean = $d_a(u_a - v_a) + 2u_a v_a h_a$

The total genetic variance will be

$$\begin{aligned}\sigma_{y_a}^2 &= d_a^2 (u_a^2 + v_a^2) + 2u_a v_a h_a^2 - [(u_a - v_a)d_a + 2u_a v_a h_a]^2 \\ &= 2u_a v_a [d_a + h_a(v_a - u_a)]^2 + 4u_a^2 v_a^2 h_a^2\end{aligned}$$

which upon summation for  $n$  such genes will be seen to equal equation [1].<sup>5</sup>

The variance for between progeny of different females is

$$\begin{aligned}\sigma_{f_a}^2 &= u_a (u_a d_a + v_a h_a)^2 + v_a (u_a h_a - v_a d_a)^2 - [(u_a - v_a)d_a + 2u_a v_a h_a]^2 \\ &= d_a^2 (u_a^3 + v_a^3 - u_a^2 - v_a^2 + 2u_a v_a) + 2u_a v_a d_a h_a (v_a - u_a) + u_a v_a h_a^2 (1 - 4u_a v_a)\end{aligned}$$

<sup>5</sup> The equivalence of  $\sigma_y^2$ ,  $\sigma_m^2$ ,  $\sigma_f^2$ , and  $\sigma_{m \times f}^2$

to equations [1-9] for within cross variance is algebraic only. Under experimental conditions the estimates of  $\sigma_y^2$ ,  $\sigma_m^2$ ,  $\sigma_f^2$ , and  $\sigma_{m \times f}^2$

will differ from the within cross estimates whenever: (a)  $u \neq v \neq \frac{1}{2}$ ;

(b) linkage influences the within cross variance; (c) where epistasis is present.

$$\begin{aligned}
&= d_a^2 \left[ u_a^3 + 1 - 3u_a + 3u_a^2 - u_a^3 - u_a^2 - v_a^2 + 2u_a v_a \right] + 2u_a v_a d_a h_a (v_a - u_a) \\
&\quad + u_a v_a h_a^2 (1 - 4u_a v_a) \\
&= d_a^2 \left[ 1 - 3u_a + 3u_a^2 - u_a^2 - (1 - 2u_a + u_a^2) + 2u_a v_a \right] + 2u_a v_a d_a h_a (v_a - u_a) \\
&\quad + u_a v_a h_a^2 (v_a - u_a)^2 \\
&= d_a^2 (-u_a v_a + 2u_a v_a) + 2u_a v_a d_a h_a (v_a - u_a) + u_a v_a h_a^2 (v_a - u_a)^2 \\
&= u_a v_a \left[ d_a + h_a (v_a - u_a) \right]^2
\end{aligned}$$

which upon summation for  $n$  such genes will be seen to equal  $\frac{1}{2}\sigma_d^2(F_2)$  in equation [2].

Similarly upon summation, the variance for between progeny of different males turns out to be

$$\sigma_m^2 = \Sigma u_a v_a \left[ d_a + h_a (v_a - u_a) \right]^2 \quad \text{and} \quad \sigma_f^2 = \sigma_m^2$$

Then the variance for the interaction will be

$$\sigma_{m \times f_a}^2 = \sigma_{v_a}^2 - (\sigma_{m_a}^2 + \sigma_{f_a}^2) = 4u_a^2 v_a^2 h_a^2$$

which when summed for a series of such genes will be found to equal  $\sigma_h^2(F_2)$  in equation [3].

The model for the mean expressions for the  $F_1$  may be used for the  $F_2$  and  $F_3$ . Only one change is necessary. The mean of the heterozygous classes becomes  $h/2$  and  $h/4$  for the  $F_2$  and  $F_3$  respectively.

In the  $F_2$

$$\sigma_m^2 = \sigma_f^2 = \Sigma u_a v_a \left[ d_a + \frac{h_a}{2} (v_a - u_a) \right]^2 = \frac{1}{2}\sigma_d^2(\bar{F}_3) \text{ in equation [5] and}$$

$$\sigma_{m \times f}^2 = \Sigma u_a^2 v_a^2 h_a^2 = \sigma_h^2(\bar{F}_3) \text{ in equation [6].}$$

In the  $F_3$

$$\sigma_m^2 = \sigma_f^2 = \Sigma u_a v_a \left[ d_a + \frac{h_a}{4} (v_a - u_a) \right]^2 = \frac{1}{2}\sigma_d^2(\bar{F}_4) \text{ in equation [8] and}$$

$$\sigma_{m \times f}^2 = \frac{\Sigma u_a^2 v_a^2 h_a^2}{4} = \sigma_h^2(\bar{F}_4) \text{ in equation [9].}$$

It is thus apparent that algebraically in the  $F_1$

$$\sigma_m^2 = \sigma_f^2 = \frac{1}{2}\sigma_d^2(F_2)$$

$$\sigma_{m \times f}^2 = \sigma_h^2 (F_2)$$

in the  $F_2$  
$$\sigma_m^2 = \sigma_f^2 = \frac{1}{2} \sigma_d^2 (\bar{F}_3)$$

$$\sigma_{m \times f}^2 = \frac{1}{4} \sigma_h^2 (F_2)$$

and in the  $F_3$  
$$\sigma_m^2 = \sigma_f^2 = \frac{1}{2} \sigma_d^2 (\bar{F}_4)$$

$$\sigma_{m \times f}^2 = \frac{1}{16} \sigma_h^2 (F_2)$$

The estimate of heritability of yield for any generation equals the additive genetic variance divided by the total variance.

$$= \frac{\sigma_m^2 + \sigma_f^2}{\sigma_m^2 + \sigma_f^2 + \sigma_{m \times f}^2 + \sigma^2}$$

### Discussion

In the proposed genetic models it is assumed that the genes at the separate loci are randomly distributed in a population of homozygous lines from which the parents were drawn at random. It has also been assumed that epistatic interactions are absent. No assumptions can be made concerning the size of  $u$  relative to  $v$  as the effects of selection, natural or otherwise, are unavoidable which would have a tendency to make  $u > v$ .

If  $h \neq 0$  and  $u > v$  the fixable portion of the additive genetic variance will have a negative bias which will, however, diminish as homozygosity is approached. Where  $h = 0$ ,  $\sigma_m^2$  and  $\sigma_f^2$  estimate  $\Sigma u_a v_a d_a^2$  regardless of the values of  $u$ . If  $\sigma_m^2 = \sigma_f^2$  is expanded, the way in which  $\Sigma u_a v_a d_a^2$  is biased when  $u \neq v$  and  $h \neq 0$  can be seen.

$$F_1 \sigma_m^2 = \Sigma u_a v_a d_a^2 + 2 \Sigma u_a v_a d_a h_a (v_a - u_a) + \Sigma u_a v_a h_a^2 (v_a - u_a)^2$$

$$F_2 \sigma_m^2 = \Sigma u_a v_a d_a^2 + \Sigma u_a v_a d_a h_a (v_a - u_a) + \Sigma u_a v_a \frac{h_a^2}{4} (v_a - u_a)^2$$

$$F_3 \sigma_m^2 = \Sigma u_a v_a d_a^2 + \Sigma u_a v_a d_a \frac{h_a}{2} (v_a - u_a) + \Sigma u_a v_a \frac{h_a^2}{16} (v_a - u_a)^2$$

For an arithmetic example, assume that  $h = d$  (complete dom-

inance). Then the three terms of  $\sigma_m^2$  take the following values as  $u$  changes for one locus. Table 4.<sup>6</sup>

TABLE 4. INFLUENCE OF CHANGES IN  $u$  ON  $\sigma_m^2$  WHERE  $h = d$ , FOR ONE LOCUS

Generation	$u$	$u_a v_a d_a^2$	$2u_a v_a d_a h_a (v_a - u_a)$	$u_a v_a h_a^2 (v_a - u_a)^2$	Total bias
$F_1$	0.5	$0.25d_a^2$	0	0	0
	0.6	$0.24d_a^2$	$-0.096d_a^2$	$0.0096d_a^2$	$-0.0864d_a^2$
	0.7	$0.21d_a^2$	$-0.168d_a^2$	$0.0336d_a^2$	$-0.1344d_a^2$
	0.8	$0.16d_a^2$	$-0.192d_a^2$	$0.0576d_a^2$	$-0.1344d_a^2$
	0.9	$0.09d_a^2$	$-0.144d_a^2$	$0.0576d_a^2$	$-0.0864d_a^2$
$F_2$	0.5	$0.25d_a^2$	0	0	0
	0.6	$0.24d_a^2$	$-0.048d_a^2$	$0.0024d_a^2$	$-0.0456d_a^2$
	0.7	$0.21d_a^2$	$-0.084d_a^2$	$0.0084d_a^2$	$-0.0756d_a^2$
	0.8	$0.16d_a^2$	$-0.096d_a^2$	$0.0144d_a^2$	$-0.0816d_a^2$
	0.9	$0.09d_a^2$	$-0.072d_a^2$	$0.0144d_a^2$	$-0.0576d_a^2$
$F_3$	0.5	$0.25d_a^2$	0	0	0
	0.6	$0.24d_a^2$	$-0.024d_a^2$	$0.0006d_a^2$	$-0.0234d_a^2$
	0.7	$0.21d_a^2$	$-0.042d_a^2$	$0.0021d_a^2$	$-0.0399d_a^2$
	0.8	$0.16d_a^2$	$-0.048d_a^2$	$0.0036d_a^2$	$-0.0444d_a^2$
	0.9	$0.09d_a^2$	$-0.036d_a^2$	$0.0036d_a^2$	$-0.0324d_a^2$

Values for other than  $h = d$  may be readily obtained by multiplying the numbers in the fourth and fifth column by  $h/d$  and  $(h/d)^2$  respectively.

For a single gene pair in the  $F_1$  the effects of  $u \neq v$  will be increased to a maximum bias due to  $h_u$  where  $h_u = \frac{-d_a}{(v_a - u_a)}$ .

This result can be obtained by setting the total bias equal to  $y$  and differentiating with respect to  $h_u$ .

<sup>6</sup> The author is indebted to Dr. R. E. Comstock for suggesting this table.

$$y = 2u_a v_a d_a h_a (v_a - u_a) + u_a v_a h_a^2 (v_a - u_a)^2$$

$$\frac{dy}{dh} = 2u_a v_a d_a (v_a - u_a) + 2u_a v_a h_a (v_a - u_a)^2$$

$$h_a = \frac{-d_a}{v_a - u_a}$$

For example, if  $d_a = 1$  and  $u_a = 0.7$ , a maximum bias due to  $h_a$  in the  $F_1$  would be obtained when  $h_a = 1/0.4 = 2.5$ . Substituting back in the original equation, we see that a value of  $h_a = 2.5$  (where  $d_a = 1$ ) will reduce  $\sigma_m^2$  to zero. Values of  $h_a$  this high would imply extreme over-dominance. Similar maximum values may be calculated for the  $F_2$  and  $F_3$ . In addition, estimates of  $\sigma_m^2 = \sigma_f^2$  may be biased where epistasis is present. This bias may be minimized by transformation of the data to a more suitable scale such as logarithms (5). Also, the bias due to epistasis will be less as the crosses become more homozygous.

### *Summary*

A model for the estimation of the components of genetic variance between self-fertilized bulked progenies from crosses of isogenic lines has been presented. The mathematical basis for the method of estimation has been presented in detail. The limiting assumptions have been briefly discussed.

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